## STRATOS Survival Analysis Subgroup

Terry Therneau

Mayo Clinic

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Current survival analysis group

- Michal Abrahamowicz
- Per Kragh Andersen
- Richard Cook
- Pierre Joly
- Torben Martinussen
- Maja Pohar-Perme

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There is obvious overlap with the initial STRATOS topic groups:

- TG1: missing data
- ► TG2: selection of variables and functional form
- ► TG3: descriptive and initial data analysis
- ► TG4: measurement error and misclassification
- TG5: study design
- ► TG6: evaluating diagnostic tests and prediction models

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► TG7: causal models

- ► TG1: missing data
- ► TG2: selection of variables and functional form
- TG3: descriptive and initial data analysis
- ► TG4: measurement error and misclassification
- TG5: study design
- ► TG6: evaluating diagnostic tests and prediction models

TG7: causal models

- TG1: missing data
- TG2: selection of variables and functional form
  - time-dependence and non-linear effects
- ► TG3: descriptive and initial data analysis
- ► TG4: measurement error and misclassification
- TG5: study design
- TG6: evaluating diagnostic tests and prediction models

TG7: causal models

- TG1: missing data
- TG2: selection of variables and functional form
- TG3: descriptive and initial data analysis
  - survival curves
  - event rates and person-years
- TG4: measurement error and misclassification
- TG5: study design
  - sample size for survival studies
  - special designs
- TG6: evaluating diagnostic tests and prediction models

TG7: causal models

- ► TG1: missing data
- ► TG2: selection of variables and functional form
- TG3: descriptive and initial data analysis
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- TG5: study design
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- ► TG7: causal models
  - ipw and marginal-structural models

# Specific topics

- Time dependent covariates: usage and pitfalls
- Time-dependent effects and flexible modeling
- Multiple events
  - competing risks and multi-state models
  - recurrent events
  - joint models of survival and longitudinal markers
- Particular models
  - Cox proportional hazards
  - additive
  - accelerated failure time, parametric and non-parametric

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- restricted mean life
- Penalized models and random effects
- Relative survival
- Interval censoring
- Causal/cumulative effects
- Validation

► Time dependent covariates

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#### Time dependent covariates

survival by treatment response, immortal time bias

- reverse causality, end of life markers
- use of midpoints for interval censored data
- ▶ ...

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- reverse causality, end of life markers
- use of midpoints for interval censored data
- ▶ ...
- Time dependent effects
  - $\beta(t) \times \text{NOT } \beta x(t)$

- Multiple events
  - Medical need

## Multiple events

- Medical need
- competing risks and multi-state

- repeated events
- joint modeling

## ► Particular models

Cox model

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#### Particular models

- Cox model
- Additive hazard

$$\flat \ \lambda_1(t)e^{X\beta} + \lambda_2(t)e^{X\gamma} + \dots$$

- Accelerated failure time
- Residual life

- $\lambda_0(t)e^{X\beta+Zb}$  $Db \sim G(0,s)$
- Classic mixed effects: D = I, G = Gaussian, general s

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- Relative survival
- Interval censoring
- Causal modeling

#### Software validation

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What is a sufficient test suite?

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